

2013

TRIAL HIGHER SCHOOL CERTIFICATE EXAMINATION

Mathematics

General Instructions

- Reading time 5 minutes.
- Working time 180 minutes.
- Write using black or blue pen.
- Board approved calculators may be used.
- Show all necessary working in Questions 11–16

Total Marks - 100 Marks

Section I 10 Marks

- Attempt Questions 1–10
- Allow about 15 minutes for this section.

Section II 90 Marks

- Attempt Questions 11–16
- Allow about 2 hour 45 minutes for this section.

Examiner: External Examiner

This is an assessment task only and does not necessarily reflect the content or format of the Higher School Certificate.

Section I

Objective-response Questions

$Total\ marks-10$

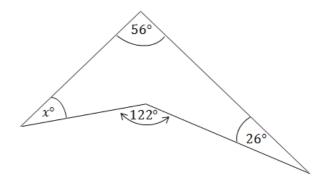
Attempt Questions 1 – 10

Answer each question on the multiple choice answer sheet provided.

1)
$$\frac{\tan^2 \theta}{1 + \tan^2 \theta} + \cos^2 \theta \text{ equals}$$

- (A) 1
- (B) $\frac{1}{2} + \cos^2 \theta$
- (C) $1 + \tan^2 \theta$
- (D) $1 + \cos^2 \theta$

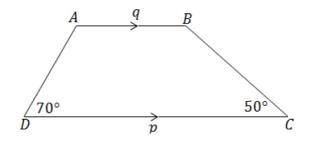
2)



In the figure above, x equals

- (A) 31°
- (B) 34°
- (C) 40°
- (D) 48°

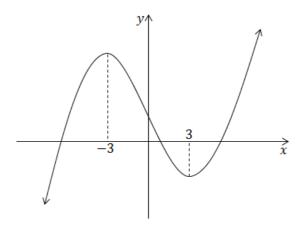
3)



In the figure above AB||DC, AB = q and DC = p.BC equals

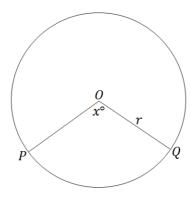
- (A) $\frac{(p+q)\sin 50^{\circ}}{2\sin 70^{\circ}}$
- (B) $\frac{(p+q)\sin 70^{\circ}}{2\sin 50^{\circ}}$
- (C) $\frac{(p-q)\sin 70^{\circ}}{\sin 60^{\circ}}$
- (D) $\frac{(p-q)\sin 50^{\circ}}{\sin 70^{\circ}}$
- 4) The period of the function $f(x) = \sin\left(3x \frac{\pi}{3}\right)$, $x \in R$ is
 - (A) $\frac{\pi}{9}$
 - (B) $\frac{2\pi}{3}$
 - (C) 2π
 - (D) $\frac{\pi}{3}$
- 5) The solution(s) of the equation $e^x + e^{-x} = -\frac{3}{2}$, where $x \in R$, is (are)
 - (A) ln 2 only
 - (B) $\pm \ln 2$
 - (C) $-\ln 2$ only
 - (D) None of these

6) From the graph of y = f(x), when is f'(x) negative?



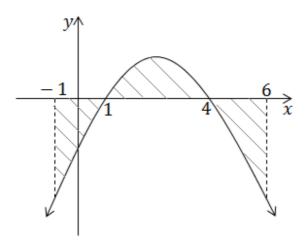
- (A) x < -3 or x > 3
- (B) -3 < x < 3
- (C) $x \le -3 \text{ or } x \ge 3$
- (D) $-3 \le x \le 3$
- 7) If M is decreasing at an increasing rate, what does this suggest about $\frac{dM}{dt}$ and $\frac{d^2M}{dt^2}$?
 - (A) $\frac{dM}{dt} < 0$ and $\frac{d^2M}{dt^2} < 0$
 - (B) $\frac{dM}{dt} > 0$ and $\frac{d^2M}{dt^2} < 0$
 - (C) $\frac{dM}{dt} < 0$ and $\frac{d^2M}{dt^2} > 0$
 - (D) $\frac{dM}{dt} > 0$ and $\frac{d^2M}{dt^2} > 0$

8)



In the figure, the radius of the sector is r and $\angle POQ = x^{\circ}$. If the area of the sector is A then x equals

- (A) $\frac{2A}{r^2}$
- (B) $\frac{360A}{\pi r^2}$
- (C) $\frac{180A}{\pi r^2}$
- (D) $\frac{180A}{r^2}$
- 9) Which of the following expressions gives the total area of the shaded region in the diagram?



- $(A) \qquad \int_{-1}^{6} f(x) \, dx$
- (B) $-\int_{-1}^{0} f(x) \, dx + \int_{0}^{6} f(x) \, dx$
- (C) $-\int_{-1}^{1} f(x) dx + \int_{1}^{4} f(x) dx \int_{4}^{6} f(x) dx$
- (D) $\int_1^4 f(x) dx + 2 \int_4^6 f(x) dx$

- 10) Which of the following is the derivative of $y = \ln[f(x)]$
 - (A) $\frac{f(x)}{f'(x)}$
 - (B) $\frac{f'(x)}{f(x)}$
 - (C) $\frac{1}{f'(x)}$
 - (D) $\frac{f''(x)}{f'(x)}$

End of Section I

Section II

Free response questions

Total marks - 90

Attempt Questions 11 – 16

Answer each question in a SEPARATE writing booklet. Extra writing booklets are available.

Question 11 (15 marks) Use a SEPARATE writing booklet.

(a) Factorise
$$x^2 - 2x + 1 - 4y^2$$

$$\sqrt{\frac{3^{5k+2}}{27^k}}$$

(c) Simplify

$$\frac{\log(a^3b^2) - \log(ab^2)}{\log\sqrt{a}}$$

(d) Solve
$$x^2 + 2x - 8 > 0$$

(e) By considering the cases $x \le 1$ and x > 1, or otherwise, solve

$$|1-x|=x-1$$

(f) For the parabola $(x-3)^2 = -4y$.

(ii) State the equation of the directrix of the parabola.

(g) Prove

$$\frac{\sin\theta}{1-\cos\theta} = \frac{1+\cos\theta}{\sin\theta}$$

(h) Evaluate

$$\lim_{x \to 2} \frac{x-2}{x^2 + x - 6}$$

2

(i) Find the equation of a straight line passing through the point of intersection of the lines l_1 : 2x - y - 4 = 0 and l_2 : 2x + 3y - 12 = 0 and perpendicular to the line 2x - 3y + 1 = 0.

(j) Find the equation of the tangent to the curve
$$y = 2 \sin 2x$$
 at the point $\left(\frac{\pi}{8}, \sqrt{2}\right)$.

Question 12 (15 marks) Use a SEPARATE writing booklet.

(a) Draw a number plane and mark the points P(-2, 2) and Q(-4, -2).

Show that the equation of the line through *P* perpendicular to *PQ* is given by x + 2y - 2 = 0

(ii) The line perpendicular to PQ through P intersects the x-axis at R. Find the coordinates of R.

(iii) Show that the mid-point of QR is (-1, -1). Mark this point T on your diagram.

- (iv) Find the perpendicular distance from T to the interval PR.
- (b) x and y are positive numbers. x, -2, y are consecutive terms of a geometric series, and -2, y, x are consecutive terms of an arithmetic series.

(i) Find the value of xy.

- (ii) Find the values of x and y.
- (iii) Find the sum to infinity of the geometric series

$$x - 2 + y$$
 ... 2

2

(c) Given that α and $m\alpha$ are the roots of the equation $x^2 + px + q = 0$, show that

$$mp^2 = (m+1)^2 q$$
 2

Question 13 (15 marks) Use a SEPARATE writing booklet.

(a) Differentiate with respect to x:

(i)
$$x \sin x$$

(ii)
$$\ln(x^2 + 4)$$

(iii)
$$e^{5x} + x$$

- (b) The graph of y = f(x) passes through the point (3, 5), and f'(x) = 2x 3. Find f(x). 2
- (c) Find:

$$\int \sqrt{x+10} \cdot dx$$

$$\int_0^{\frac{\pi}{8}} \sec^2 2x \cdot dx$$

(d) Consider the curve $y = \cos 2x$:

(i) Sketch
$$y = \cos 2x$$
 for $0 \le x \le 2\pi$.

- (ii) Find the area between the curve $y = \cos 2x$ and the x-axis from x = 0 to $x = \pi$.
- (e) The population P of Newcastle after t years is given by the exponential equation

$$P = 50000e^{-0.08t}$$

- (i) Find the time to the nearest year for the initial population to halve.
- (ii) Find the number of people who leave Newcastle during the tenth year. 2

1

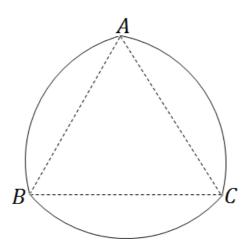
(f) A continuous curve y = f(x) has the following properties for the closed interval $-3 \le x \le 5$: f(x) > 0, f'(x) > 0, f''(x) < 0. Sketch a curve satisfying these conditions.

Question 14 (15 marks) Use a SEPARATE writing booklet.

- (a) Given that $f(x) = x(x-2)^2$
 - (i) Show that $f'(x) = 3x^2 8x + 4$.
 - (ii) Find 2 values of x for which f'(x) = 0, and give the corresponding values of f(x).
 - (iii) Determine the nature of the turning points of the curve y = f(x).
 - (iv) Sketch the curve y = f(x) showing all essential features.
 - (v) Use your sketch to solve the inequation $x(x-2)^2 \ge 0$.
- (b) An economist predicts that over the next few months, the price of crude oil, *p* dollars a barrel, in *t* weeks time will be given by the formula

$$P = 0.005t^3 - 0.3t^2 + 4.5t + 98$$

- (i) What is the price at present, and how rapidly is it going up?
- (ii) How high does she expect the price to rise?
- (c) A coin is made by starting with an equilateral triangle ABC of side 2 cm. With centre A an arc of a circle is drawn joining B to C. Similar arcs join C to A and A to B.



- (i) Find, exactly, the perimeter of the coin.
- (ii) Find area of one of its faces.

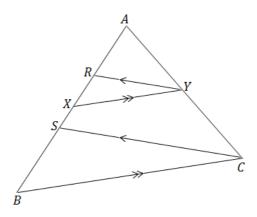
2

2

2

Question 15 (15 marks) Use a SEPARATE writing booklet.

(a) Given that in $\triangle ABC$, XY || BC and RY || SC,



Prove AX: XB = AR: RS.

2

2

2

- (b) A couple plan to buy a home and they wish to save a deposit of \$40 000 over five years. They agree to invest a fixed amount of money at the beginning of each month during this time. Interest is at 12% per annum compounded monthly.
 - (i) Let \$P be the monthly investment. Show that the total investment \$A after five years is given by

$$A = P(1.01 + 1.01^2 + \dots + 1.01^{60})$$

- Find the amount \$P needed to be deposited each month to reach their goal. (ii) Answer correct to the nearest dollar.
- A train is travelling on a straight track at 48 ms⁻¹. When the driver sees an amber light (c) ahead, he applies the brakes for a period of 30 seconds, producing a deceleration of $\frac{1}{125}t(30-t)$ ms⁻², where t is the time in seconds after the brakes are applied.
 - (i) Find how fast the train is moving after 30 seconds.

2

2

(ii) How far it has travelled in that time.

2

- (d) Two ordinary dice are thrown. Find the probability that the sum of the numbers on the uppermost faces is at least 10.

- (e) Consider the function $f(x) = x^2 \ln x \frac{x^2}{2}$:
 - Show that $f'(x) = 2x \ln x$. (i)

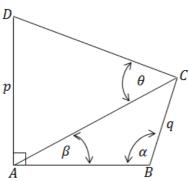
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Hence find $\int_1^2 x \ln x \, dx$. (ii)

2

Question 16 (15 marks) Use a SEPARATE writing booklet.

(a)



ABCD is a quadrilateral with *AD* perpendicular to *AB*. Given that $\angle CAB = \beta$, $\angle ABC = \alpha$, $\angle ACD = \theta$, AD = p and BC = q.

(i) Show that $\angle ADC = 90 - (\theta - \beta)$

1

(ii) Using the sine rule, prove that

3

1

$$q = \frac{p \sin \beta \cos(\theta - \beta)}{\sin \theta \sin \alpha}$$

(b) Consider the function $y = f(x) = 1 + e^{2x}$.

(i) Find f(0), f(1), f(2).

(ii) Show that $x = \frac{1}{2} \ln(y - 1)$.

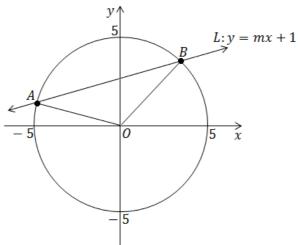
(iii) The volume V formed when the area between $y = 1 + e^{2x}$, the y-axis, and the lines y = 2 and y = 4 is rotated about the y-axis is given by:

$$V = \frac{\pi}{4} \int_{2}^{4} [\ln(y - 1)]^{2} \, dy$$

Use Simpson's rule with 3 function values to estimate this volume. Leave your answer rounded to 3 significant figures.

Question 16 continues on the next page

(c)



In the above figure, the line L: y = mx + 1 cuts the circle $x^2 + y^2 = 25$ at two points $A(x_1, y_1)$ and $B(x_2, y_2)$.

(i) Show that
$$x_1$$
 and x_2 are the roots of $(1 + m^2)x^2 + 2mx - 24 = 0$.

(ii) Show that area of
$$\triangle OAB = \frac{1}{2}(x_2 - x_1)$$
.

End of paper.

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STANDARD INTEGRALS

$$\int x^n dx = \frac{1}{n+1} x^{n+1}, \quad n \neq -1; \quad x \neq 0, \text{ if } n < 0$$

$$\int \frac{1}{x} dx = \ln x, \quad x > 0$$

$$\int e^{ax} dx = \frac{1}{a} e^{ax}, \quad a \neq 0$$

$$\int \cos ax dx = \frac{1}{a} \sin ax, \quad a \neq 0$$

$$\int \sin ax dx = -\frac{1}{a} \cos ax, \quad a \neq 0$$

$$\int \sec^2 ax dx = \frac{1}{a} \tan ax, \quad a \neq 0$$

$$\int \sec ax \tan ax dx = \frac{1}{a} \sec ax, \quad a \neq 0$$

$$\int \frac{1}{a^2 + x^2} dx = \frac{1}{a} \tan^{-1} \frac{x}{a}, \quad a \neq 0$$

$$\int \frac{1}{\sqrt{a^2 - x^2}} dx = \sin^{-1} \frac{x}{a}, \quad a > 0, \quad -a < x < a$$

$$\int \frac{1}{\sqrt{x^2 - a^2}} dx = \ln\left(x + \sqrt{x^2 - a^2}\right), \quad x > a > 0$$

$$\int \frac{1}{\sqrt{x^2 + a^2}} dx = \ln\left(x + \sqrt{x^2 + a^2}\right)$$

NOTE: $\ln x = \log_e x$, x > 0

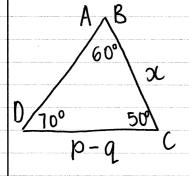
2013 MATHEMATICS TRIAL - SOLUTIONS (2-UNIT)

A

C

C

- 1. $\frac{\tan^2 \theta}{1 + \tan^2 \theta} + \cos^2 \theta$ = $\frac{\tan^2 \theta}{\sec^2 \theta} + \cos^2 \theta$ = $\sin^2 \theta + \cos^2 \theta$
- 2. 122° = x° + 56° + 26° 122° = x° + 82° x° = 40°
- 3. Eliminate AB:



- $\frac{\chi}{\sin 70^{\circ}} = \frac{p-q}{\sin 60^{\circ}}$ $\chi = \frac{(p-q)\sin 70^{\circ}}{\sin 60^{\circ}}$
- 4. $f(x) = \sin(3x \frac{\pi}{3})$ Period = $\frac{2\pi}{3}$
- 5. $e^{x} + e^{-x} = -\frac{3}{2}$ None of these

- 6. f'(x) < 0
 - -3 4 26 4 3
- B
- 7. $\frac{dM}{dt} < 0$ and $\frac{d^2M}{dt^2} > 0$ or $\frac{dM}{dt} < 0$ and $\frac{d^2M}{dt^2} < 0$
- 8. $A = \frac{\chi}{360} \chi \pi \chi r^{2}$ $\frac{360 A}{\pi r^{2}} = \chi$
- 9. $A = \int_{-1}^{1} f(x) dx + \int_{1}^{4} f(x) dx$ - $\int_{4}^{6} f(x) dx$
- 10. $y = \ln [f(x)]$ $y' = \frac{f'(x)}{f(x)}$
- D

2 unit Trial 2013 $(f) \left(\chi - 3 \right)^2 = -4y$ (x-k)=4a(y-k)(i) h = 3, k = 0, a = 1 $(\alpha-1-2y)(x-1+2y)$ 0 $\bigvee \left(3,0\right) \cdot \widehat{D}$ (b) $\sqrt{\frac{3^{5k+2}}{3^{3k}}} = \left(\frac{5^{k+2}-3^k}{3^{2k+2}}\right)^{\frac{1}{2}} = 3^{k+1}$ (c) loga + logb2 - (loga + logb2) loga 2 directrix y=+1 1 3 loga + 21/g b - loga - 21/og b $(9) \frac{\sin \theta}{\sin \theta} = 1 + \cos \theta$ 1 log a 1-0050 SIND $\frac{2\log \alpha}{\frac{1}{2}\log \alpha} = 40$ LHS $\underline{\sin\theta}_{x}(1+\cos\theta) = \underline{\sin\theta}(1+\cos\theta)$ $(1-\cos\theta)$ $(1+\cos\theta)$ $1-\cos^2\theta$ = <u>sind(14050)</u> (d) $x^{2} + 2x - 8 > 0$ SINTO $(\chi+4)(\chi-2)>0$ = 1+cos0 = RHS. 2 $\lim_{\Omega \to 2} \frac{(\chi - 2)}{(\chi + 3)(\chi - 2)}$ x<-4 and x>2. ① > = 0 (e) |1-3c| = 3c-| $1-x=x-1 \quad \text{or} \quad -(1-x)=x-1$ But for x>1, |1-x|=|x-1| 16 $\begin{array}{ll}
\lambda = 2x & -1 + x = x - 1 \\
x = 1 & 0 = 0
\end{array}$ also true Test x=1, LHS /0/=0 So x=/so(x>1) is the RHS 1-1=0

11 (1)
$$2x-y-4=0$$

 $2x+3y-12=0$
 $-4y+8=0$
 $4y=8 \Rightarrow y=2$
So $2x-2-4=0$
 $2x-6=0$
 $x=3$
Pt of Intersection (3,2)

NOW
$$2x-3y+1=0$$

 $2x+1=3y$
 $y=\frac{2}{3}x+\frac{1}{3}$
Line $1=\frac{1}{3}x+\frac{1}{3}$

11 (j)
$$y = 2 \sin 2x$$

 $y = 2 \cos 2x \times 2i$
 $= 4 \cos 2x$
 $2 \cos 2x$
 $2 \cos 2x$
 $3 \cos 2x$
 $4 \cos 4x$
 $= 4 \cos 4x$
 $= 4$

QUESTION 12. 24.2013 TRIAL.

$$(-2/2)$$
 $(-1/2)$ $(-4/2)$

$$M po = 2 - 2 = 4 = 2. \\
 -2 - 4 = 2$$

$$Me_1 = -\frac{1}{2}$$
 $P(-2,2)$

$$e_1$$
: $y-2=-\frac{1}{2}(x-2)$.

 $2y-4=-x-2$.

ijbohen
$$y=0$$
 $x=2$ or crosses at $(2,0)$

$$III)MPQR = \left(-\frac{4+2}{2}, -\frac{2+0}{2}\right)$$

$$= \left(-1, -1\right)$$

$$(x+2y-2)=0 \quad (-1,-1)$$

$$d = \left| \frac{a \times 1 + b y_1 + c}{\sqrt{a^2 + b^2}} \right| = \frac{1(-1) + 2(-1) - 2}{\sqrt{1^2 + 2^2}} = \frac{-5}{\sqrt{5}} = -\sqrt{5}$$

$$\hat{x}, -\alpha, y \quad \text{geo}. \quad \frac{-2}{x} = \frac{y}{2} = \alpha$$

-2 y x arith
$$y--2=x-y=d$$

$$2y-x+2=0$$
.

$$\frac{8}{3} - x + 2 = 0.$$

$$8 - x^2 + 2x = 0$$

$$x^2 - 2x - 8 = 0$$

$$(x^{2}-4x+2x-8)$$

$$x(x-4)+2(x-4)$$

$$(x+2)(x-4)=0$$

$$x=(4)$$
 or (-2) = $(-2,2)$ = $(-2,2)$

$$(x-2+y)$$

$$(4-2+1)$$
. $\Gamma = \frac{-2}{4} = \frac{1}{2}$

$$a=x$$
 $r=-\frac{2}{x}$

$$S_{\infty} = \frac{4}{1 - \frac{1}{2}} = 2\frac{2}{3}$$

$$S_{\infty} = \frac{Q}{1-\Gamma} = \frac{x}{1-\frac{2}{x}} = \frac{3}{4}$$

$$\frac{x}{x+2} \div = x^2 - S_{\infty} = 2\frac{2}{3}$$

$$(x-x)(x-mx)$$

$$x^2 + px + q$$

$$m\beta^{2} = (m+1)^{2}q$$

$$\alpha + m\alpha = -P$$

$$\alpha + m\alpha = -P \cdot \left[\text{Hearrange} \cdot \alpha \neq 1 + m \right] = -P$$

$$m\alpha^2 = q$$

$$_{00}^{\circ} \alpha = \frac{-\rho}{1+m}$$

$$m\left(\frac{(+p)^2}{(1+m)^2}\right) = q$$

$$mp^2 = q(1+m)^2$$

13. (a)
(i)
$$y = 2(\sin x)$$

 $dy = x \cdot \cos x + \sin x$

$$(u) y = \ln(x^2 + 4)$$

$$\frac{dy}{dx} = \frac{2x}{x^2 + 4}$$

$$(iii) y = e^{5x} + x$$

$$dy = 5e^{5x} + 1.$$

(b)
$$f(x) = 2x - 3$$

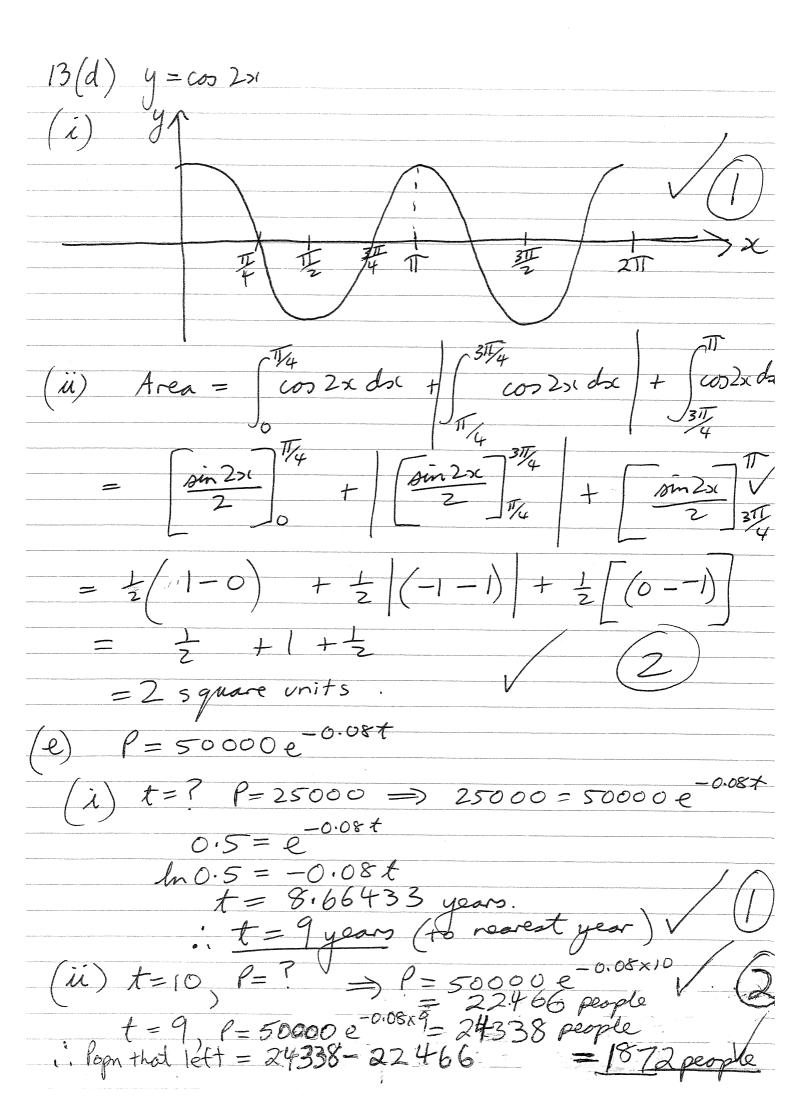
 $f(x) = x^2 - 3x + C$
 $f(3) = 5 \Rightarrow 5 = 9 - 9 + C \Rightarrow C = 5$
 $f(x) = x^2 - 3x + 5$.

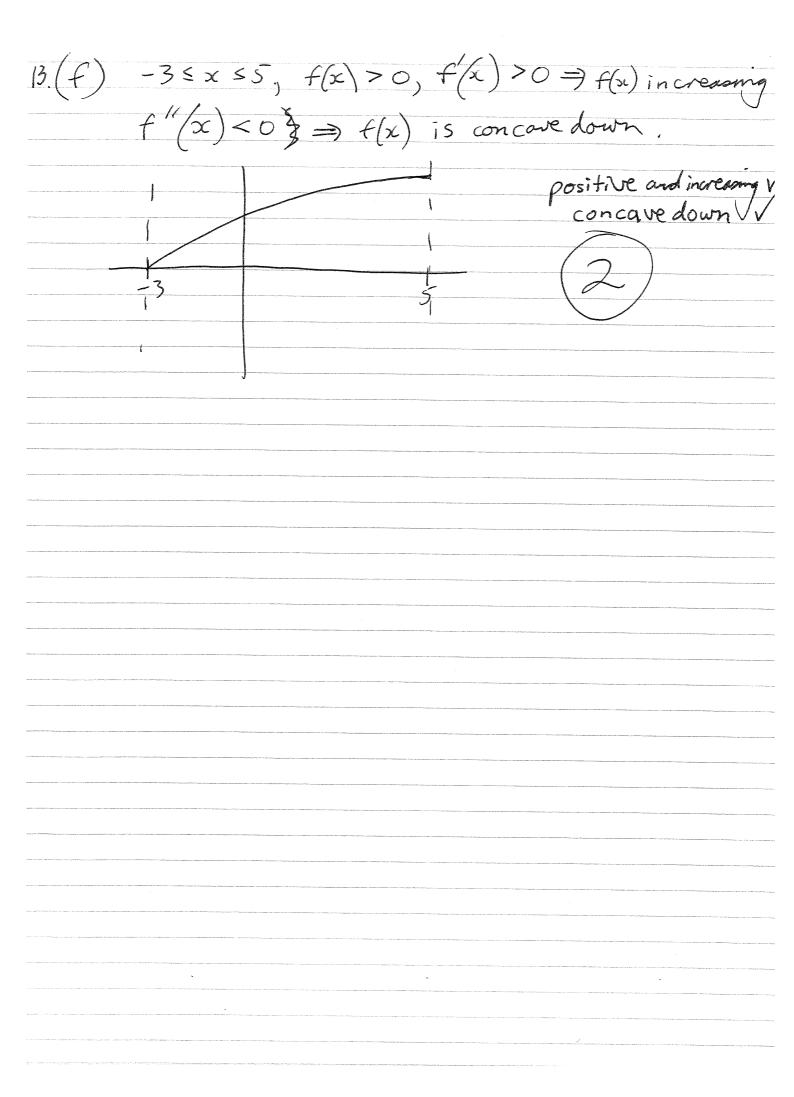
$$(c)(i) \int \sqrt{x+10} \, dx$$

$$= \frac{2(x+10)^{3/2}}{3} + C$$

$$= \frac{2\sqrt{(x+10)^3}}{3} + C.$$

(ii)
$$\int_{0}^{\sqrt{8}} \sec^{2} 2x \, dx = \left[\frac{1}{2} \tan 2\right]_{0}^{\sqrt{8}}$$
 ($=\frac{1}{2} \left[\tan \frac{\pi}{4} - \tan 0\right] = \frac{1}{2} \left(1-0\right)$





QUESTION FOURTEEN. MATHEMATICS 2013

e) i
$$f(x) = x(x-2)^2$$

= $x^3 - 4x^2 + 4x$
 $f'(x) = 3x^2 - 8x + 4$

ii)
$$f(z) = 0$$

when $3x^2 - 8x + 4 = 0$
 $(3x - 2)(x - 2) = 0$
 $x = 2$, $y = 0$
 $x = 2$, $y = 32$

in
$$f''(x) = 6x - 8$$

= $4 = 4 \text{ when } x = 2$. MIN
= $-4 = 2/3 = 2/3 = 4 \times 10^{-2}$

w-)

i) When
$$t=0$$
 $P = 98, 198

$$\frac{aP}{at} = .015 t^2 - .6t + 4.5$$
When $t=0$, $\frac{dP}{dt} = 4.5$, $t + 4.50$

ii)
$$\frac{df}{dt} = 0$$
 when
$$\frac{3}{300}t^{2} - \frac{6}{10}t + \frac{9}{2} = 0$$

$$3t^{2} - 120t + 900 = 0$$

$$t^{2} - 40t + 300 = 0$$

$$(t - 10)(t - 30) = 0$$

$$t = 10,30$$

$$\frac{d^2 P}{o U} = -0.3 t - 0.6$$

$$= -0.3 \text{ iden } a = 10$$
Hence Relative MAX.

When t = 10, P = 118

NOTE
A relative maximum occurs
when t=10 but chene is no
appecific given domain so
P= D as t increases
HOWEVER

next few months" so the inference is t=10 weeks.

When t=10, P = 118, \$118

$$\begin{array}{c|c}
A & & \\
\hline
CIRCLE & \\
CIRCLE & \\
C & O = T_3
\end{array}$$

i) Perimeter consists of 3 ares p = 3 NO= 3 NO

= 2 T cm.

ii) Area consents of

1 taingle + 3 reg ments

A = \(\frac{1}{2} r^2 \text{Sen 0 + 3 x \(\frac{1}{2} r^2 \text{0 - ring} \)} \)

= \(\frac{3}{2} r^2 \text{0 - r^2 \text{Sen 0}} \)

-3 x4 x 5 - 4 53

= 271 - 2 \(\sigma \) in \(\)

= 2 (T- \(\sigma \) cm

(a AX:XB = A4:4C (proportional

(b) (i) Amt after I month = 1x1.01

Ant after 2 months = Px1.012 + Px1.07

Ant after 3 months = (P x 1.012 + Px1.01) x1.01 + Px1.01

: A = Amt after 60 months = P(101 + 1.01 + --- + 1.01)

a required 2

(ii)
$$A = \frac{P \times 1.01 \times (1.01^{60} - 1)}{1.01 - 1}$$

:40000 = Px101x(1.0160-1)

= 484.9286 __ -

(c) $\ddot{x} = -\frac{t}{125}(30-t)$

$$=\frac{c^2}{125}-\frac{6t}{25}$$

$$\dot{x} = \frac{t^3}{375} - \frac{3t^2}{25} + C$$

When t=0 48 = C

$$\vec{x} = \frac{t^3}{375^2} - \frac{3t^2}{25} + 48$$

$$2.x = \frac{t^4}{1500} - \frac{t^3}{25} + 48t + C,$$

When
$$t=0: 0 = c_1$$

$$\therefore x = \frac{t^4}{1500} - \frac{t^3}{25} + 48t$$

(i) when
$$t = 30$$
, $x = \frac{30^3}{375} - \frac{3 \times 30^2}{25} + 48$
= 12 mc⁻¹

d)
$$P(4t | east | 10) = P(10) + P(10) + P(10)$$

= $P(46,55,44) + P(56,65) + P(10)$
= $\frac{6}{36}$
= $\frac{1}{6}$

(e)
$$f(x) = x^2 \ln x - \frac{x^2}{2}$$

(i)
$$f'(x) = \ln x \cdot 2x + x^2 \cdot \frac{1}{x} - \frac{2x}{2}$$

= $2x \ln x + x - x$
= $2x \ln x$

(ii)
$$\int_{1}^{2} x \ln x \, dx = \frac{1}{2} \int_{1}^{2} 2x \ln x \, dx$$
$$= \frac{1}{2} \left[x^{2} \ln x - \frac{x^{2}}{2} \right]_{1}^{2}$$

=
$$\frac{1}{2}$$
 [4 $\ln 2 - \frac{4}{2}$] - $\left[1.0 - \frac{1}{2}\right]$

$$= \frac{1}{2} \left\{ 4 \ln 2 - 2 + \frac{1}{2} \right\}$$

$$=242-\frac{3}{4}$$

Question 16 THSC 2 vn. 2. (a)(i) LACB= 180-(2+B) (L Sum)

(ii) 1 = AL sing = AL sing = AL sing = AL

4 a = AC SIND ACE PSIND

= psin DsinB sind sind.

(3) Sin D= sin(90-6-p) = cos(0-B)

= $p \leq n \beta \cos(\theta - \beta)$ Sino sind.

(b)(i)
$$f(0)=1+1=2$$

 $f(1)=1+e^{2}$
 $f(2)=1+e^{4}$

(ii)
$$y = 1 + e^{2\pi}$$

$$e^{2\pi} = y - 1$$

$$2x = \ln(y - 1)$$

$$7x = \frac{1}{2} \ln(y - 1)$$

 $\approx 0.819 \text{ units}^3$

(c)(i)
$$y_1 = mx_1 + 1$$
 (D) are true since (x_1, y_1)
 $x_1^2 + y_1^2 = 250$ is on both cures.

$$(14m^{2})\chi_{1}^{2} + 2m\chi_{1} - 24 = \chi_{1}^{2} + m^{2}\chi_{1}^{2} + 2m\chi_{1} + 1 - 25$$

$$= \chi_{1}^{2} + (m\chi_{1} + 1)^{2} - 25.$$

$$= \chi_{1}^{2} + (y_{1}^{2} - 25from)$$

$$= 25 - 25 \quad from(2)$$

$$= 0.$$

Similarly for 22.

(ii)

Area =
$$\frac{1}{2} \times (\times (-\chi_{1}) + \frac{1}{2} \times 1 \times \chi_{2}$$

= $\frac{1}{2} (\chi_{2} - \chi_{1})$.