**Gosford High School** 

## 2014

TRIAL HIGHER SCHOOL CERTIFICATE EXAMINATION

# **Mathematics**

- General Instructions
- Reading time 5 minutes
- Working time 3 hours
- Write using black or blue pen Black pen is preferred
- Board-approved calculators may be used
- A table of standard integrals is provided at the back of this paper
- In Questions 11 16, show relevant mathematical reasoning and/or calculations

### Total Marks – 100

#### 10 marks

- Attempt Questions 1 10
- Allow about 15 minutes for this section



#### 90 marks

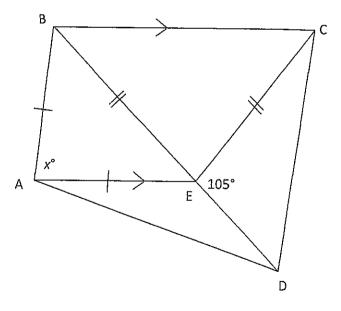
- Attempt Questions 11 16
- Allow about 2 hours and 45 minutes for this section

sction I

10 marks Attempt Questions 1 – 10. Allow about 15 minutes for this section.

Use the multiple-choice answer sheet for Questions 1 - 10.

- 1. An engine under development contains three components that are prone to failure. The probilities that each of the components will fail are  $\frac{1}{10}$ ,  $\frac{1}{5}$  and  $\frac{1}{4}$  respectively. What is the probability that at least one part will fail?
  - (A)  $\frac{23}{50}$
  - (B)  $\frac{1}{200}$
  - (C)  $\frac{3}{100}$ (D)  $\frac{11}{20}$
- 2. The vertices of quadrilateral ABCD meet at E such that BC||AE, BE is produced to D.  $\angle CED = 105^{\circ}$ , BE = CE and AB = AE. Determine the size of x.
  - (A) 105°
  - (B) 85°
  - (C) 75°
  - (D) 52.5°



- - -

3. Fully simplify the algebraic fraction:  $\frac{x^3 - 8}{x^2 - 4}$ .

(A)  $\frac{x^2 - 2x + 4}{x - 2}$ 

(B)

(C)  $\frac{x^2 + 4x + 4}{x + 2}$ 

*x* + 2

(D) 
$$\frac{x^2 + 2x + 4}{x + 2}$$

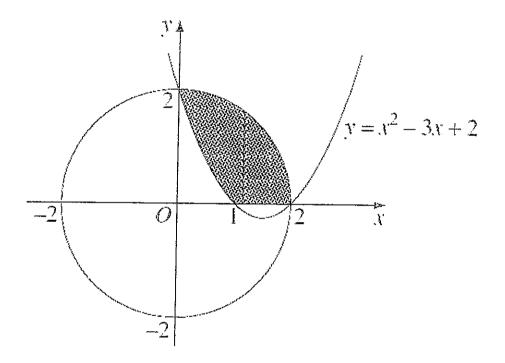
4. What is the value of  $\frac{dy}{dx}$  if  $y = 4\sqrt{x}$ ?

- (A)  $\frac{dy}{dx} = 4$
- (B)  $\frac{dy}{dx} = 2\sqrt{x}$
- (C)  $\frac{dy}{dx} = \frac{2}{\sqrt{x}}$
- (D)  $\frac{dy}{dx} = -\frac{1}{2\sqrt{x}}$
- 5. During a two year study, the number of people using public transport increased by 6% in the first year and in the following year the number increased by a further 14% to 680 000. The number of people using public transport at the beginning of the study was approximately:
  - (A) 8 095
  - (B) 549 712
  - (C) 562 728
  - (D) 544 000
- 6. The quadratic function  $3x^2 6x 7$  has roots  $\propto$  and  $\beta$ . What is the value of  $\propto^2 + \beta^2$ ?
  - (A)  $\frac{26}{3}$
  - (B)  $-\frac{7}{3}$
  - (C) 4
  - (D) 45

1.

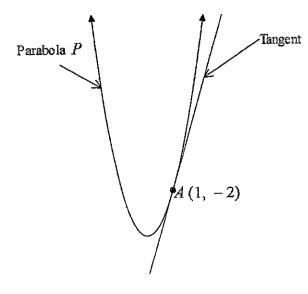
The primitive function of  $\sec^2 5x + 1$  is:

- (A)  $\frac{1}{5}\tan(5x) + x + C$
- (B)  $\frac{1}{5}\tan(x) + 5x + C$
- (C)  $\tan(5x) + x + C$
- (D)  $\tan(5x) + C$
- 8. Which set of inequalities best describes the shaded region.



- (A)  $x^2 + y^2 \le 2$  and  $y \ge x^2 3x + 2$  and  $y \ge 0$
- (B)  $x^2 + y^2 \le 4$  and  $y \le x^2 3x + 2$  and  $x \ge 0$
- (C)  $x^2 + y^2 \le 2$  and  $y \le x^2 3x + 2$  and  $y \ge 0$
- (D)  $x^2 + y^2 \le 4$  and  $y \ge x^2 3x + 2$  and  $x \ge 0$

9. The diagram shows the parabola P and its tangent at the point A(1, -2).



Which of the following equations might represent the normal to the parabola at the point A?

$$(A) \quad x-3y+5=0$$

(B) 
$$2x - 3y + 1 = 0$$

(C) 
$$x + 3y + 5 = 0$$

$$(D) \quad x+3y-5=0$$

10. Differentiate 
$$\log_e\left(\frac{x-5}{x+5}\right)$$

(A) 
$$\frac{25}{x^2-25}$$

(B) 
$$\frac{10}{x^2-25}$$

(C) 
$$\frac{1}{x-5} + \frac{1}{x+5}$$
  
(D)  $\frac{1}{x+5} - \frac{1}{x-5}$ 

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Loon II

#### 90 marks

Attempt Questions 11-16.

## Allow about 2hours and 45 minutes for this section.

Answer each question in the appropriate writing booklet. Extra writing booklets are available.

In Questions 11 - 16, your responses should include relevant mathematical reasoning and/or calculations.

## Question 11 (15 marks) Start on a new page.

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(a)	Evaluate $\log_{10} 12$ correct to 3 significant figures.	1

(b) Solve 
$$|2x - 3| = 4 - 3x$$
 2

- Differentiate the following functions with respect to *x*: (c)
  - $3xe^x$ (i)

1

1

(ii) 
$$\frac{1}{(x^2+5)^3}$$
 1

(iii) 
$$\frac{x^2+4}{3x-1}$$
 1

(d) If 
$$f'(x) = 6x^2 + 5x - 1$$
 and  $f(-1) = 5$ , find an expression for  $f(x)$ .

A particle moves so that its displacement from the origin is given by: (e)

> $x = -t^2 + 7t + 8$ (where x is displacement in metres and t is time in seconds) What is the initial displacement of the particle? (i)

- (ii) At what time will the particle be at the origin? 2
- Consider the arithmetic sequence beginning with -7, -3, 1 ...: (f)

.1

(i)	Find the 25 <sup>th</sup> term in the sequence.	1
(ii)	Show that the sum of the first 20 terms is 620	1
(iii)	How many terms must be taken to give a sum of 221?	2

#### End of Question 11

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Question 12 (15 marks) Start on a new page.

- (a) Sammy sailed 15km south from point A to point B. He then sailed due west to C where he was on a bearing of 210° from A.
  - (i) Draw a diagram showing this information.
  - (ii) Determine the exact distance AC

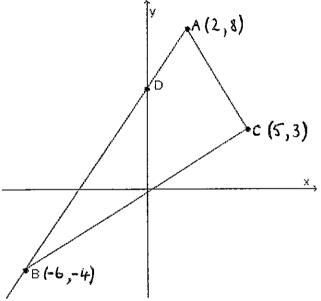
(iii) Sammy then sailed NW for 8km to D. What is the distance from A to D correct to the nearest 100m.

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(b) The points A(2, 8), B(-6, -4), and C(5, 3) are the vertices of triangle ABC.



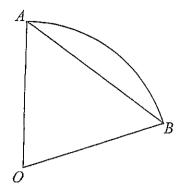
(i)	Find the equation of the line passing through A and B.	4
(ii)	Find the coordinates of the point D.	1
(iii)	Find the perpendicular distance from point $C$ to the line $AB$ .	2
(iv)	Find the exact distance between A and B.	2
(v)	Calculate the area of $\triangle ABC$ .	1

#### Question 12 continues on page 9

## Question 12 (continued)

(i)

(c) Sector AOB has arc length  $AB = 2\pi$  units and radii OA = OB = 6 units.



Determine the size, in radians, of angle  $A\hat{O}B$ .

1

1

(ii) Show that the area of  $\triangle AOB$  is  $9\sqrt{3}$  square units.

End of Question 12

Question 13 (15 marks) Start on a new page.

(a)	A function is given by $f(x) = -x^3 + \frac{3x^2}{2} + 6x$							
	(i) Find the coordinates of the stationary points of $f(x)$ and determine their nature.							
	(ii) Find the coordinates of the point of inflexion of $f(x)$ .	1						
	(iii) Hence, sketch the graph $y = f(x)$ showing the stationary points, point of inflexion and y intercept.	3						
	(iv) For what values of $x$ is the function decreasing?	1						
(b)	Consider the function $f(x) = 4 \sin 2\pi x$							
	(i) Determine the period and amplitude of $f(x)$	2						
	(ii) Determine the values of x for which $f(x)$ is at its maximum in the domain $0 \le x \le 2$	2						
	(iii) Sketch $f(x)$ for $0 \le x \le 2$ .	1						
(c)	Evaluate: $\lim_{x \to 2} \frac{3x^2 - 12}{x - 2}$	2						

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## End of Question 13

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Question 14 (15 marks) Start on a new page.

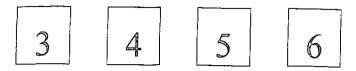
(a) Use Simpson's rule to approximate  $\int_{1}^{5} \frac{dx}{x^2+1}$ , using 4 sub-intervals to 4 decimal places.

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(b) Four cards, numbered 3, 4, 5 and 6 are used in a game.

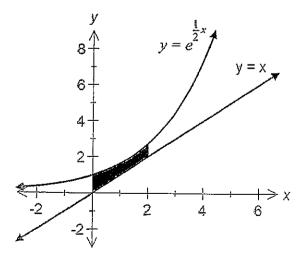


The four cards are placed face down and each player pays \$1 to take a turn to draw two cards, one at a time without replacement. The two cards make a 2-digit number, with the first card drawn being the first digit of their number.

If the cards form a number over 60, the player receives \$3 back (i.e. they win \$2), otherwise they receive nothing back.

The four cards are then shuffled and replaced for the next turn.

- (i) Use a diagram to show all of the possible 2-digit numbers that could be drawn. 2
- (ii) What is the probability that a player will win on their first turn?
- (iii) Calculate the probability that a player who brings \$5 to play will have \$3 left after 5 turns?
- (c) The diagram shows the graphs of the functions  $y = e^{\frac{1}{2}x}$  and y = x. The region between 3 these 2 functions and the bounds x = 0 and x = 2 has been shaded.



Calculate the exact area of the shaded region.

#### Question 14 continues on page 12

## Question 14 (continued)

- (d) For the parabola with equation  $16y = x^2 4x 12$ :
  - (i) Find the coordinates of the vertex.
  - (ii) Find the coordinates of the focus.
  - (iii) Find the equation of the directrix.

## End of Question 14

2

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Question 15 (15 marks) Start on a new page.

- (a) The population of New South Wales in 2009 was 7.13 million. In 2012 the population had grown to approximately 7.3 million people.
  - (i) Assuming that the growth rate is proportional to the population, show that the annual growth rate is approximately 0.79%.

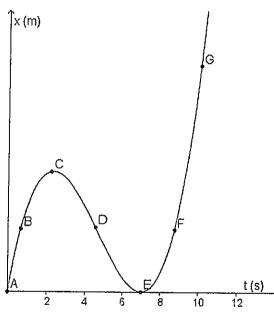
2

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- (ii) Calculate the expected population of New South Wales in 2019 using this model.
   Give your answer rounded to the nearest hundred thousand.
- (iii) In what year will the population exceed 10 million?
- (b) The graph shows the displacement (x metres) of a particle at time (t seconds). The particle is moving horizontally.



- (i) At which point, during the first 8 seconds is the particle at its maximum distance from the origin?
- (ii) Describe the motion of the particle at 4 seconds in terms of its displacement and velocity.
- (iii) By referring to the points marked on the graph, between what times is the acceleration of the particle negative? What feature of the graph tells us this?

## Question 15 continues on page 14

## Question 15 (continued)

(c) Find the solutions to the equation:

$$4\cos^2\theta = 6\sin\theta + 6$$
 in the domain  $0 \le \theta \le 2\pi$ 

(d) Show that 
$$\frac{1}{\sqrt{n} + \sqrt{n+1}} = \sqrt{n+1} - \sqrt{n}$$
 for all integers  $n \ge 1$ .

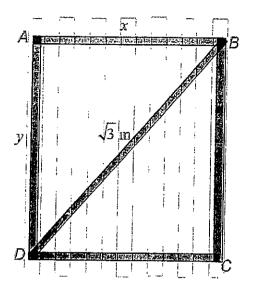
End of Question 15

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Question 16 (15 marks) Start on a new page.

A swinging gate is to be constructed from timber palings. It will require a support frame (a) using 5 pieces of timber: AB, AD, BD, BC and CD.

AB || CD and AD || BC. AB = CD = x metres. AD = BC = y metres. BD is  $\sqrt{3}$  metres long.



- (i) Find an expression for y in terms of x.
- Show that the <u>total length</u> (L) of the timber pieces in the support frame is (ii) represented by  $L = 2\left(x + \sqrt{3 - x^2} + \frac{\sqrt{3}}{2}\right)$ . 1

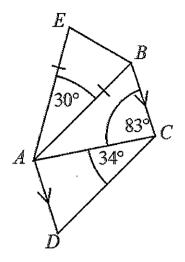
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The gate will have its maximum strength when the <u>total length</u> (L) of its support (iii) 4 frame is maximised. For what value of x will the gate have maximum strength? Full working must be shown.

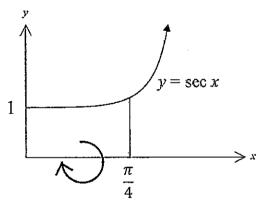
#### Question 16 continues on page 16

## Question 16 (continued)

(b) In the diagram below: AD||BC, AE = AB,  $\angle BAE = 30^{\circ}$ ,  $\angle BCA = 83^{\circ}$ ,  $\angle ACD = 34^{\circ}$ ,  $\angle EBC = 138^{\circ}$ .



- (i) Prove that  $AB \parallel DC$ .
- (ii) Prove that  $\triangle ABC \equiv \triangle ACD$ .
- (c) The area bounded by the function  $y = \sec x$ , the y-axis and the line  $x = \frac{\pi}{4}$  is rotated about the x-axis.



3

3

3

Find the volume of the solid formed.

End of Paper

## STANDARD INTEGRALS

$$\int x^n dx = \frac{1}{n+1} x^{n+1}, \quad n \neq -1; \quad x \neq 0, \text{ if } n < 0$$

$$\int \frac{1}{x} dx = \ln x, \quad x > 0$$

$$\int e^{ax} dx = \frac{1}{a} e^{ax}, \quad a \neq 0$$

$$\int \cos ax dx = \frac{1}{a} \sin ax, \quad a \neq 0$$

$$\int \sin ax dx = -\frac{1}{a} \cos ax, \quad a \neq 0$$

$$\int \sec^2 ax dx = \frac{1}{a} \tan ax, \quad a \neq 0$$

$$\int \sec^2 ax dx = \frac{1}{a} \tan ax, \quad a \neq 0$$

$$\int \sec ax \tan ax dx = \frac{1}{a} \sec ax, \quad a \neq 0$$

$$\int \frac{1}{a^2 + x^2} dx = \frac{1}{a} \tan^{-1} \frac{x}{a}, \quad a \neq 0$$

$$\int \frac{1}{\sqrt{a^2 - a^2}} dx = \sin^{-1} \frac{x}{a}, \quad a > 0, \quad -a < x < a$$

$$\int \frac{1}{\sqrt{x^2 - a^2}} dx = \ln \left(x + \sqrt{x^2 - a^2}\right), \quad x > a > 0$$

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NOTE:  $\ln x = \log_e x, x > 0$ 

## **Trial HSC Examination 2014**

## **Mathematics** Course

Name\_\_\_\_\_ Teacher \_\_\_\_\_

## Section I - Multiple Choice Answer Sheet

## Allow about 15 minutes for this section

Select the alternative A, B, C or D that best answers the question. Fill in the response oval completely.

Sample:	2 + 4 =	(A) 2	(B) 6	(C) 8	(D) 9
		AO	B 🐨	сO	d O

If you think you have made a mistake, put a cross through the incorrect answer and fill in the new answer.



If you change your mind and have crossed out what you consider to be the correct answer, then indicate the correct answer by writing the word correct and drawing an arrow as follows.

					correct		
			A 🕱		в 🗯	сO	DO
1.	A 🔿	B 🔿	C ()	D 🔿			
2.	$A \bigcirc$	вO	C ()	D 🔿			
3.	$A \bigcirc$	в 🔿	с 🔿	D 🔿			
4.	$A \bigcirc$	вO	C 🔿	D 🔿			
5.	$A \bigcirc$	вO	C ()	D 🔿			
6.	A 🔿	B 🔿	C ()	D 🔿			
7.	A 🔿	вO	C ()	D 🔿			
8.	$A \bigcirc$	в 🔿	C ()	D 🔿			
9.	$A \bigcirc$	вO	C ()	D 🔿			
10.	$A \bigcirc$	вO	C 🔿	D 🔿			

ଞ 0 2 0 - = 5762727.57-- $\frac{10 \cdot \frac{d}{dx} \left( x + 5 \right)}{dx} = \frac{d}{dx} \left( \frac{x-5}{x+5} \right) - \frac{d}{dx} \left( \frac{x-5}{x+5} \right) - \frac{d}{dx} \left( \frac{x+5}{x+5} \right)$ 5. Alumber x 1,06 x 1.14 = 680,000 1.06×1.14 12723 € anniber = 650 000 いキン - X+5 - X+5 4 NB 1 とん = (2) - 2 (-2)  $\frac{\kappa^{2} + \beta^{2}}{\kappa^{2} + \beta^{2}} = (\kappa + \beta)^{2} - 2\kappa\beta$ = = fan 5x 1. x + c. = 4 + 14 Sec 5x+1 due 3x7-62-7 -3-26 K+B=-5 م ف ر 4 1  $\overline{a}$  $\overline{\mathbb{O}}$ Ŀ' 8 s. -Solutions LEGL = LELB (Equal base engles of 150cerles & EBS opposite equal sides) LABE = LAEB (Equal base and es et waveles 143 E appose to LAEB - LCBE (Alterate angles on Rc/1AE are equa-20+52-57 +52-55 - 1800 (. A.g. un of d. ×=75° (c) = 52.5° equal sectors). 6 2 3- 8 \_ (2 2) (2 2 + 2 2 + 4) 2014 Trial 45C - Mathemakies 1.  $P(z, t, t_{n,i}) = 1 - P(0, t_{n,i})$ =  $1 - (\frac{1}{2} \times \frac{z}{5} \times \frac{z}{5})$ (2+2) (2+2) J x++2x+4 LEBC - 52.5° 842 - 50 = 52.50 dy = Lx42 4 |12 |12 4 - 4 x 7 1 ל, <del>ג</del> 8 4

Check د) لن . <u>6)</u>\_\_\_ a(E) LHS # RHS ~ ~ ~ ~  $LHS = \frac{12(\frac{7}{5})-3}{2}$ 00 30 2x - 3 = 4 - 3x22-3 - 4-32 da 22 00 ų 5~ -7 2 2 2 1 7+4 12 = 1.07918. 3×-1 (22-25) × = 1.08 (3 s.g. hjs, (3xex) = 3xex 3ex is the only solution. ψ 11 v ų =3ex(x+1)  $\frac{(3x-1) \times 2x - 3(x^2+4)}{x^2}$ x - 2x - 3x - 12 25 - 6x (x + 5)# -3 (x2+5) × 2x R ŝ Les = Rets (3x-1-) R + s = 4 - 3(t)(3 - 1) LHS > 1 (x2+5)=3 -(2x-3)=4-32 -2x+3 - 4-32 ų 12(1)-3 א יי e) (1) Initial displacement t:0 Ē : f(x) = 6x + 5x - x + c f (x) = 6 x + 5x - 1 F(-1) = 5  $\frac{(-1)^{2}}{5} = \frac{2(-1)^{3}}{5} + \frac{5(-1)^{2}}{5} - (-1) + C$ 5= 12+0 C = 3 2  $f(m) = 2m^3 + \frac{5}{2}n^2 - n + \frac{7}{2}$ Particle at origin = 2 = 0 = 2x<sup>3</sup> + 5x<sup>2</sup> - x + C x = 8  $\chi = -(\delta)^{2} + 7(\delta) + 8$ But t20 0 = (+ - 8)(+ + 1)  $o = t^2 - 7t - 8$ 0 = - t + 7 + + 8 E= -1,8 ٢  $\frac{=3x^{2}-2x-12}{(3x-1)^{2}}$ |, |-| t=8 seconds.

LN, CA = LBAC = 30° (Alteriate angles on , 20cA = 30°+ 45° (10 is NW of 2) DA = 8 + + (10, 13) - 2 (8 ) (10, 53 ) Cas 75 = 17.1 km (reacest lop m) = 10 J3 km Ac = 2x15 12 ۴ ۲ Cos 30 = 15 = 292.2739, DA = 17.0960 ... - 32 -(i) Let 0 = LCA3 0 + 180 = 210° 15 km Or = 30 Γω 9 z  $|\underline{R}, \underline{a}, \underline{(l)}_{N}|$  $\int_{20}^{\infty} = \frac{20}{2} \left[ 2 \left( -7 \right) F \left( 20 - 1 \right) (4) \right]$  $(\hat{u}) \quad S_n = \frac{\alpha}{2} \left[ 2\alpha + (\gamma - i) \delta \right]$ Sn = 2 [2a+ (n-1)d]  $T_{x} = a + (n - 1) d$  $T_{25} = -7 + (25 - 1)x +$  $\frac{2}{(n-1)} \frac{2}{(2n+1)} = 0$ × ا ا 212-91-221=0 442= 412-18m 4. -18n - 442=0 but 170 = 120 - 89 a = ~7 

= 17 <u>13</u> with		$\frac{dz}{az, tby tc}$	00	(11) D 1 72=0 3(0) -2y +10=0 2y =10 y =5	2y -16 = 3x -6 3x -2y +10 =0	b) (i) $y - y_1 = \frac{y - y_1}{x_2 - x_1} (x - x_1)$ $A(2, 8) B(-6, -4)$ $y - 8 = \frac{-4 - 8}{-6 - 2} (x - 2)$ $y - 8 = \frac{3}{2} (x - 2)$
	$= 9\overline{13} w^2$	$= \frac{1}{2} \times \frac{1}{2} \times \frac{1}{2}$	$\frac{3}{(ii) A = \frac{1}{2} \circ b \sin c}$		n 11	(v) $A = \frac{\sqrt{(26)^2 + (8'4)^2}}{= \sqrt{8^2 + 12^2}}$ = $\sqrt{8^2 + 12^2}$ = $\sqrt{208}$ = $\sqrt{208}$ = $\sqrt{13}$ units.

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< 0 - - magamm f"(a) = - 16 T 2 Sin 2 Tr  $\frac{f^{*}(u)}{z} = -it\pi^{2}Si^{*}(2\pi^{2}t)$  $f''(x) = - (i\pi^2 S_{\mathcal{A}}(2\pi(\xi)))$ 2 < -1 and x>2 - 0 = 1, <u>31</u>, <u>51</u>, 6 = 8 m Cus 2 m x O = Cas 24 m b) f(x)= 4 Sin 2mm (24.6, 2.0) 212 = 3I (1) Amplihuele = 4 Perioel = 1 -2 = 4 ---х " " Sther - M Cos @= 0 f (2) 20 -(ii)-----0 ł ·· (2, 10) is a local munum  $At = x = 2, \quad y = -(2)^3 + 3(2)^2 + 4(2).$  $A^{\mu} = -l_{\gamma} - \frac{1}{2} = -(-1)^{3} + \frac{3(-1)^{n}}{2} + 6(-1)^{3}$ 3 Check: x  $-\frac{1}{2} - \frac{1}{2} - \frac{1}{2} - \frac{1}{2} + \frac{3}{2} - \frac{1}{2} + \frac{1}{2} - \frac{1$ (ii) Point of interior f"(2)=0 13. a (i) \_ f (n)= - 2'+ 32 - + 62 f'(x)=-3x2+3x+6 Stationary Peints f(x) = 0  $f_{-1}^{-1}(x_{-}), z_{-} = -6(-t_{-}), t_{-}3$ 0 = -3 x - + 3 x + 6  $f''(\kappa) = -6(\iota) r3$ 0=(2-2)(2+1) 0=-6(2)+3 0 = x - x - 2 f "(x) = -6x+3. -3 -- 6 2 (0.5,3.25) = 3.25 2 - 2

. с) lun x+2 ج ک Period = 1 Local merining at 2 = 4 , 1+4 3x2-12 オーン ~!~ ~!~ ļρ. μ 4 2 オークレ lim 3(2+2) ł 3 (2+2)(2-2 x = 1 - 5 2 6 (iii)  $(\mathbf{\tilde{E}})$ 4 0 151 Ξ 3  $\frac{P(l_{win}, \mu_{losses}) = \frac{1}{4} \times \left(\frac{3}{4t}\right)^{+}}{= \frac{4}{1024}}$ 1 א<sup>7</sup> לא \$0 remaining / win = +\$3 i 4 losses Start with \$5. P(w) = +5 turns cost 5x\$1 5 53 54 X 56 fa 3 X 54 35 34 6 63 64 65 X א 3456  $dx = \frac{1}{3} \left[ 0.5 + \frac{1}{(0.2 + \frac{1}{12})} + 2(0.1) + \frac{1}{25} \right]$ 0.5 0.2 0.1 12 36 1+ x Carol. = 0.591251 .... ļ ł 2 5163.0 در dise ¥ ×S h (4 d. p. ļ

= 7.7 ×106 (Nearest hundred thousand . स् ....t = 0 ... N= 7.13 x10' L=3 N=7.3 x10 - Uning the # (2001 + 43) year N=7.13×00 6.0018×10 = 0.79 % (2 d. p.) - 0.0078543. 10 × 10 = 7.13 × 10 2 0.0071 t  $7.3 \times 10^{2} = 7.13 \times 10^{6} \frac{3^{4}}{6}$  $\frac{3k}{3k} = \frac{\lambda_n}{\lambda_n} \left( \frac{\gamma_{\cdot3}}{\overline{\gamma_{\cdot3}}} \right)$  $\frac{k}{k} = \mathcal{L}\left(\frac{7.3}{7.13}\right)$ Less  $t = l \cdot \left(\frac{10}{7!3}\right)$ = 43.068 ... 6100.0 = 7.3 7.13 10 ... e 2074 = 10 7.13 2019 -> t=10 140.00 4 6 - 3 N= Aeke <u>(1) (1) (1)</u>  $(\tilde{e})$ ξ} Concare up  $= \left(2e^{\frac{1}{2}(2)} - 2e^{\frac{1}{2}(2)}\right) - \left(\frac{(1)^{1}}{2} - \frac{(0)^{2}}{2}\right)$ x dr z dez de l z do  $(i) - 16y = (x - 2)^{2} - 4 - 12$ (iii) Ducehix y = -1-4  $(ii) \frac{4a = 16}{a = 4}$ ----- (2, 3) ----d) 16y=x2-4x-12 = 2(e-2) ~<sup>2</sup> 1 1 2  $\frac{16\left(\frac{1}{2}+1\right)=(2e-2)^{2}}{2}$ e sk 1<u>64 +16 = (x-r)<sup>r</sup></u> Verley al (2,1) = 2e - 4 .c) <u>A=</u>

c) 4 cos 0 = 6 sin 0 + 6 (III) Between points A and D. The graph is incare down during this time. (ii) At 45, it is in a positive direction from the origin (right) and has a negative velocity (moving towards the origin, b)\_\_\_(i)\_\_\_ C 4 - 45in 0 - 65in 0 - 6 = 0 But ofosar Let re= Sin @ -4 sin 20-6550-2 = 0 4 (1-sin 20) = 6 sin 0 + 6 -4x2-6z-2=0 . (2x+1)(x+1) -0 22+32+1 =0 Jun 10- - -Siff = - 1  $\theta = \frac{1}{1} + \frac{1}{2}, 3\pi + \frac{\pi}{2}, \dots$ 日= サ+2 \* = - ! - | 21-7-7-31+7-47-7-(Sin # = 1 1 + 1 + 1 N + 1 JN - JN+1 2 - 2+ łı μ ģ 1/21 - 27 <u>17 - 17+1</u> Vn - (n+) (1+0) - 01

 $d^{2} - \frac{1}{2} = -2 - 2 - \frac{1}{2} - \frac{1}{2}$  $z - 2x^{2} (3 - x^{2})^{\frac{3}{2}} - 2 (3 - x^{2})^{-\frac{3}{2}}$ mIN  $(3 - \frac{3}{2})$  $\sqrt{(3-x^2)}$ <u>dl = 2 - 2 ~ (3 - 2 ~ ) - 2</u> Menum Strength when 2 = 0 / · · · 2 ] 3 m But 2 >0 (leigh 4 | | | | | Check it's a massimin of 2 (2 - 2 - 2) } an  $\frac{d^{2}L}{du^{2}} = -\frac{2\left(\frac{2}{2}\right)}{\sqrt{\left(3-\frac{2}{2}\right)^{3}}}.$ = -3.26S - - 2% maximum When x= (3 0 √  $\frac{dL = 2\left(1 + \frac{1}{2}(3-x^2)^{-\frac{1}{2}}x^2x\right)}{du}$  $L = 2 \left( \chi + \left( 3 - \chi^2 \right)^2 + \frac{J_3}{2} \right)$  $L = 2(2c + \sqrt{3-2c^2} + \frac{\sqrt{3}}{2})$ Stationery pourt: de = c = 2 - 2x  $\frac{y_{z}}{z} \sqrt{(5)^{2}-x^{2}}$   $\frac{y_{z}}{z} \sqrt{3-x^{2}}$   $\frac{L^{2}}{z} \frac{2}{x} + 2y + \sqrt{3}$   $\frac{z}{z}$ 2m = 2 3-22 0 = 2 + 2x 422 - 4. (322) 4 2 - - 12 - 42 a) (i)  $(\sqrt{3})^{2} = \varkappa^{2} + \eta^{2}$ Sub y= J3-x2 82== 12 <u></u>3-75

. 1 ..... ; : .... . . . . . . : S ; . . . . . . . . . (n) (n) . ..... . . . . ..... : 1 . . . . . . . • • • • • • • ..... ...... . ...... : 1 : -----: WABC = ACDA (AAS) ķ But A Þ : 2 LABE + 30 = 180 (L sin of 1 180) V= N In A ABC and ACOA, = m tan I - tan of = Tr [tan n]# LAES = LABE (l LABC + LBCD = 63+83+34 48 110c ₹ ABE A-c is common LBCA = LOAC = 83° LBACE LOCA = 34° (Alternate engles on ABILOC : LABE = 75" Sec. × dre - LABC = 138-75 + LABC = 138° ( Cointerior angles and to 180°) - 180 (Equal angles apposite equal sides-A = + B (Curin)) = 63° (Alternate angles on AD 1135) . (LEBC = 138 (church)